Flux-Emergence Model for the Characterization of Solar Active Regions

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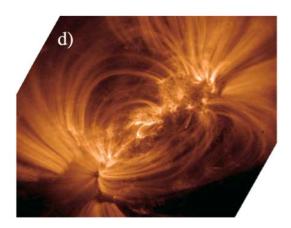


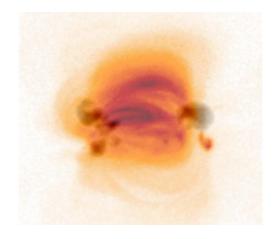
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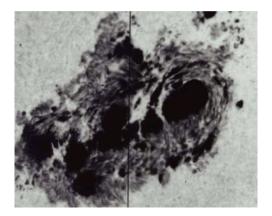
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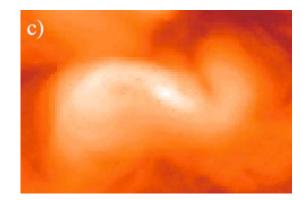


There are various types of solar active regions...



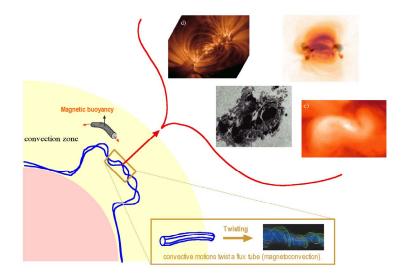






Similarity between solar active regions and animals...

Active regions



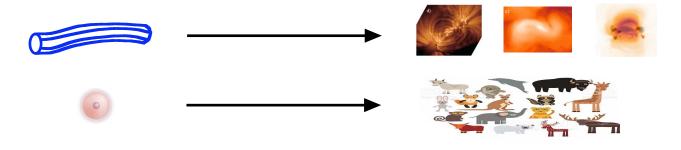
Animals



https://www.istockphoto.com/jp/%E3%83%99%E3%82%AF%E3%82%BF%E3%83%BC/%E7%94%9F%E7%89%A9%E3%81%AE%E9%E 0%82%E5%8C%86%E3%81%AB%E3%82%B9%E3%82%AD%E3%83%BC/%E3%83%BC/%E7%94%9F%E7%89%A0%E3%81%AE%E9%E3%81%95 animalschilden-%E3%81%AE%E6%55%99%E3%82%B2%F2%747%91%E5%A0%A6%E3%81%AE%E3%81%99_m463713287338481

Their origins have simple structure.

Even though they have simple structure, these origins play fundamental roles in determining the characteristics of active regions/animals.

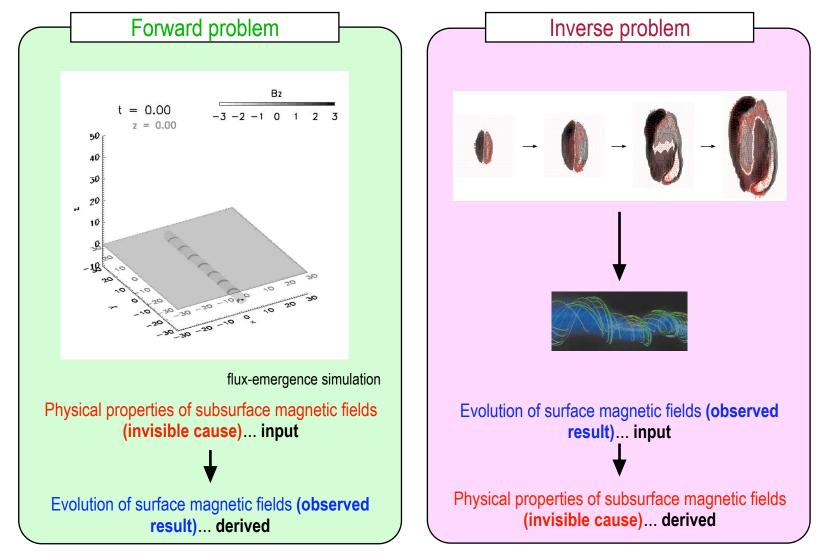


This suggests that physical properties of subsurface magnetic fields (twisted flux tube) characterize solar active regions.

However, it is difficult to obtain these properties <u>via direct</u> <u>observations using electromagnetic waves</u> (the surface of the Sun behaves like an impermeable boundary toward radiative flux).

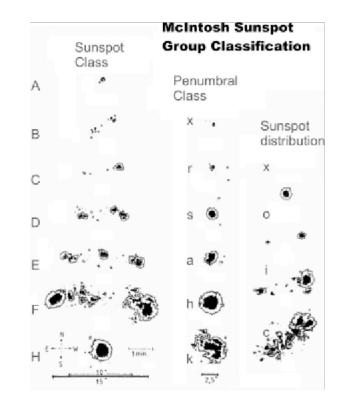
Then what shall we do?

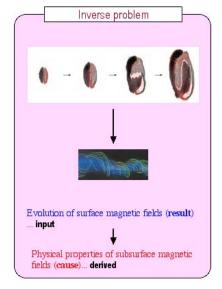
Forward problem vs. Inverse problem



By solving the inversion problem, we may derive physical properties of subsurface magnetic fields.

Surface magnetic fields have been classified on the basis of their morphological features.





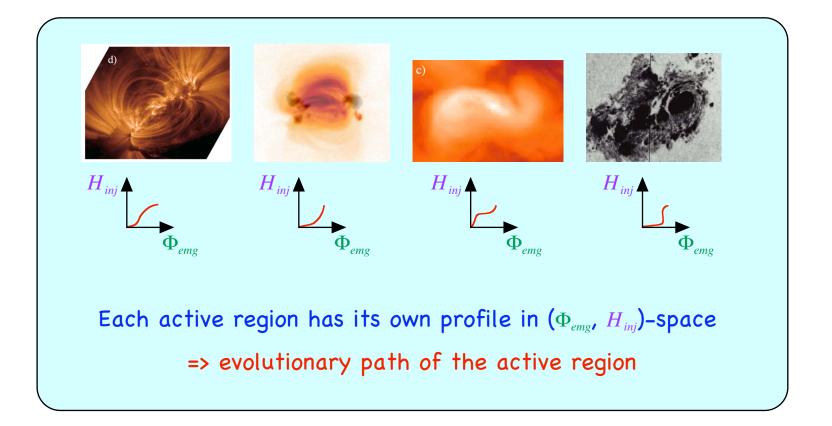
For solving the inverse problem, such morphological classification is insufficient to provide an input in the problem.

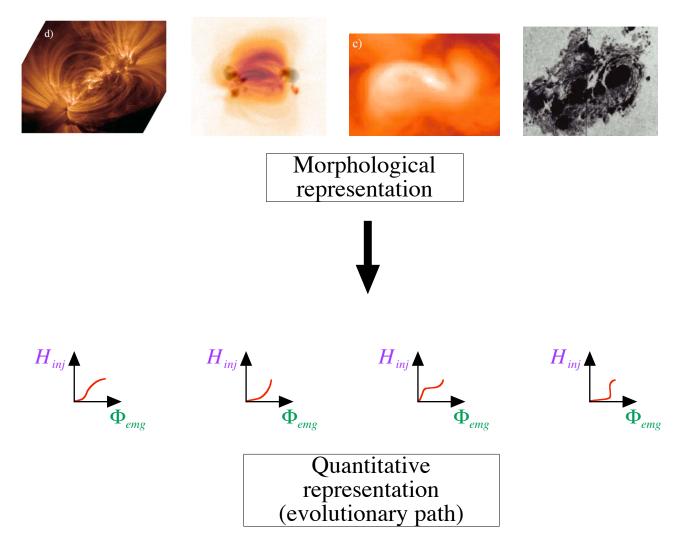
A quantitative representation of surface magnetic field evolution is necessary.

Quantitative representation of surface magnetic field evolution

Two key quantities obtained from observations of surface magnetic field evolution:

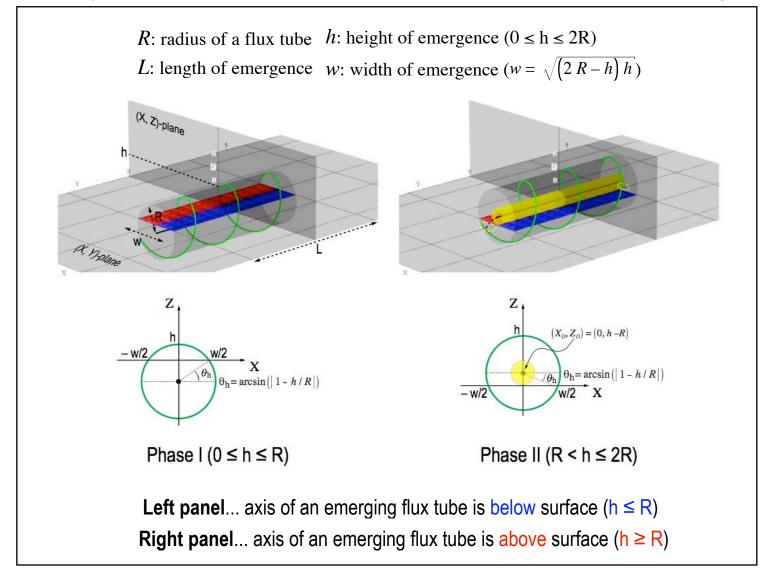
Emerged magnetic flux (Φ_{emg})... provides information on scales **Injected magnetic helicity** (H_{ini})... provides information on configurations





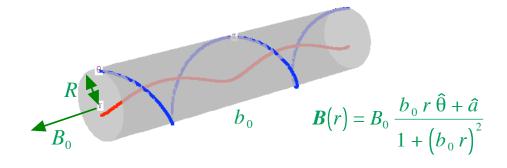
Using the evolutionary path, we solve the inverse problem.

To derive physical properties of subsurface magnetic fields from the evolutionary path via inversion, we introduce a model of flux emergence.

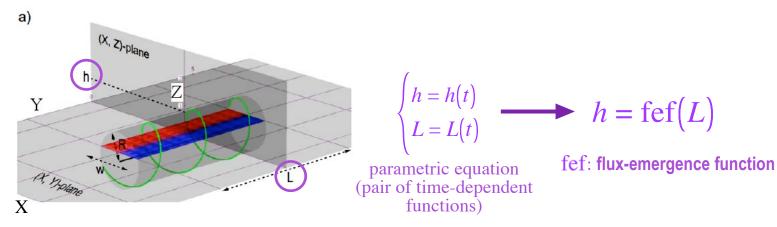


The model provides key physical parameters that describe the properties and processes of subsurface magnetic fields...

Physical properties of subsurface magnetic fields: flux-tube radius, field strength, twist



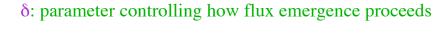
Time-dependent processes of flux emergence: emergence length, emergence height

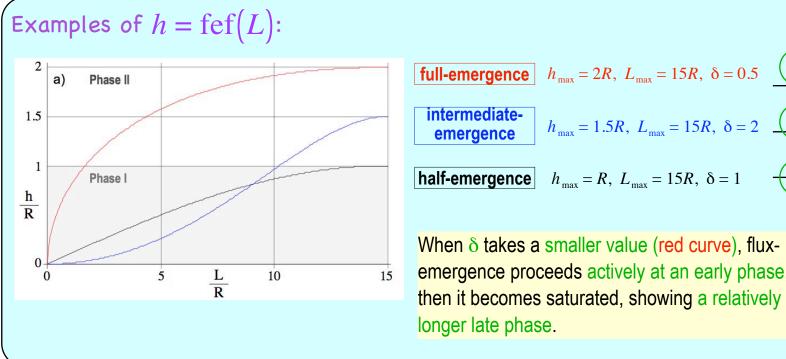


Flux-emergence function... characterized by three parameters

$$h = \operatorname{fef}(L) = h_{\max} \sin \left[\frac{\pi}{2} \left(\frac{L}{L_{\max}} \right)^{\delta} \right]$$

h_{max}: maximum emergence height L_{max}: maximum emergence length





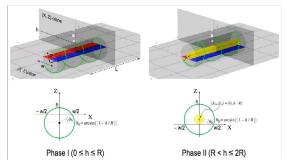
_	full-emergence $h_{\text{max}} = 2R, \ L_{\text{max}} = 15R, \ \delta = 0.5$
_	intermediate- emergence $h_{\text{max}} = 1.5R, \ L_{\text{max}} = 15R, \ \delta = 2$
	half-emergence $h_{\text{max}} = R, \ L_{\text{max}} = 15R, \ \delta = 1$
	When δ takes a smaller value (red curve), flux- emergence proceeds actively at an early phase,

Emerged magnetic flux & injected magnetic helicity calculated from the model...

Emerged magnetic flux (Φ_{emg}):

• Apparent emerged flux (Φ_{emg}^{A}) ... signed flux crossing a horizontal plane (surface): directly observed

 $\Phi_{emg}^{A}(\text{Phase I}) = \frac{B_{0} \boldsymbol{L}}{|b_{0}|} \ln \left(\frac{1 + b_{0}^{2} R^{2}}{1 + b_{0}^{2} (R - \mathbf{h})^{2}}\right)^{A}$ $\Phi_{emg}^{A}(\text{Phase II}) = \frac{B_{0} \boldsymbol{L}}{|b_{0}|} \ln \left(\frac{1 + b_{0}^{2} R^{2}}{\left[1 + b_{0}^{2} (R - \mathbf{h})^{2}\right]^{1 - \frac{2\pi}{|b_{0}|L}}}\right)$



• Net emerged flux (Φ_{emg}^{N}) ... unsigned flux crossing a vertical plane:

used for calculating injected magnetic helicity

Injected magnetic helicity (*H*_{inj}):

$$H_{inj} (\text{Phase I}) = \frac{B_0^2 L}{4 b_0^3} \left((\pi - 2 \theta_h) \left\{ \ln \left(1 + b_0^2 R^2 \right) \right\}^2 - \int_{\theta_h}^{\pi - \theta_h} \left\{ \ln \left(1 + \frac{b_0^2 (R - h)^2}{\sin^2 \theta} \right) \right\}^2 d\theta$$

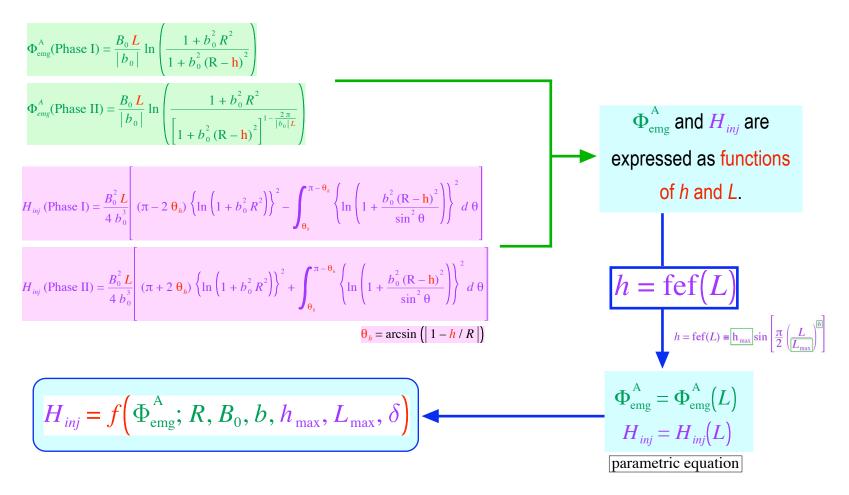
$$H_{inj} (\text{Phase II}) = \frac{B_0^2 L}{4 b_0^3} \left((\pi + 2 \theta_h) \left\{ \ln \left(1 + b_0^2 R^2 \right) \right\}^2 + \int_{\theta_h}^{\pi - \theta_h} \left\{ \ln \left(1 + \frac{b_0^2 (R - h)^2}{\sin^2 \theta} \right) \right\}^2 d\theta$$

$$\theta_h = \arcsin \left(\left| 1 - h / R \right| \right)$$

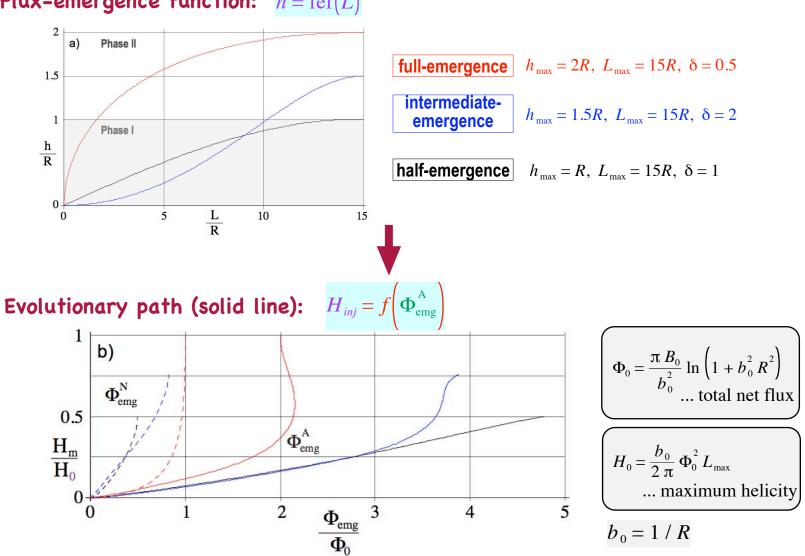
A set of six parameters in the model determine the evolutionary path of an active region...

Physical properties of subsurface magnetic fields: R, B_0, b_0

Time-dependent processes of flux emergence: $h_{
m max}, L_{
m max}, \delta$

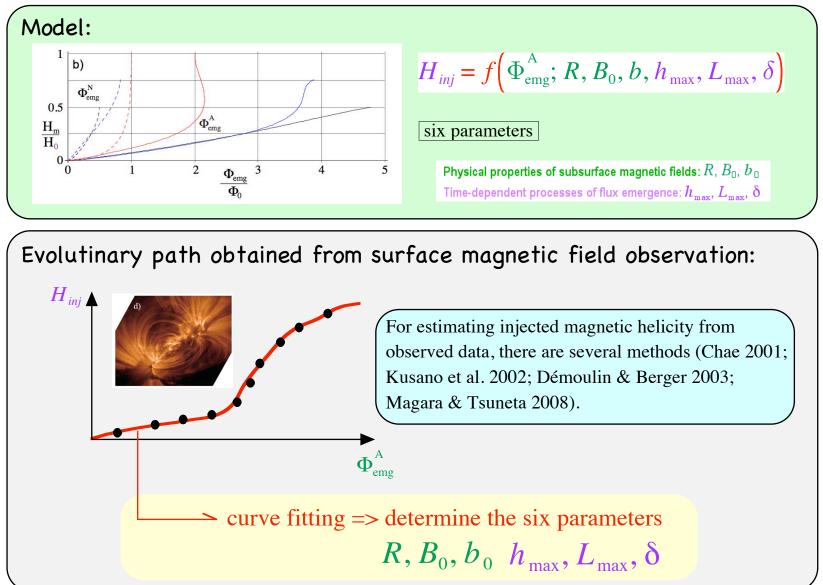


Examples of the evolutionary path...



Flux-emergence function: h = fef(L)

Inversion (curve-fitting analysis)...



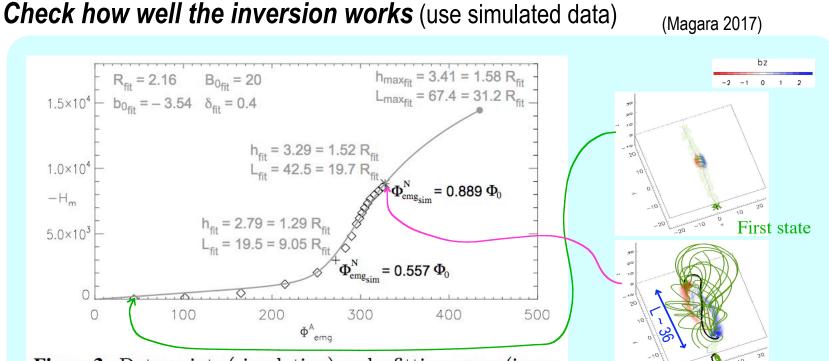


Figure 3. Data points (simulation) and a fitting curve (inversion) are presented in (Φ_{emg}^A, H_m) -space, which are drawn in black and gray, respectively. + and * show a half-emergence state and the state shown by right panel of Fig. 1b.

	simulation	inversion	ſ
R	2	2.16	
B ₀	17.4	20	
b ₀	 – 1 (left-handed twist) 	- 3.54	
L	~ 36 (final state)	42.5	

A possible explanation of this discrepancy is that after they emerge, magnetic field lines tend to be twisted strongly <u>around their</u> <u>footpoints at the surface</u>, which may enhance the inversion value compared to the uniform twist value assumed initially in the simulation.

End state