

Structure of the Sun

Core... 0 ~ 160,000 km

Energy is generated by nuclear fusion.

T : 15,800,000 K (center)

Radiative zone... 160,000 km ~ 500,000 km

Energy is transported by radiation.

Convection zone... 500,000 km ~ 700,000 km

Energy is transported by convection.

Photosphere... 0 ~ 500 km (solar surface = 0 km)

Observed in visible light (solar surface)

T : 6000 K

Chromosphere... 500 km ~ 2000 km

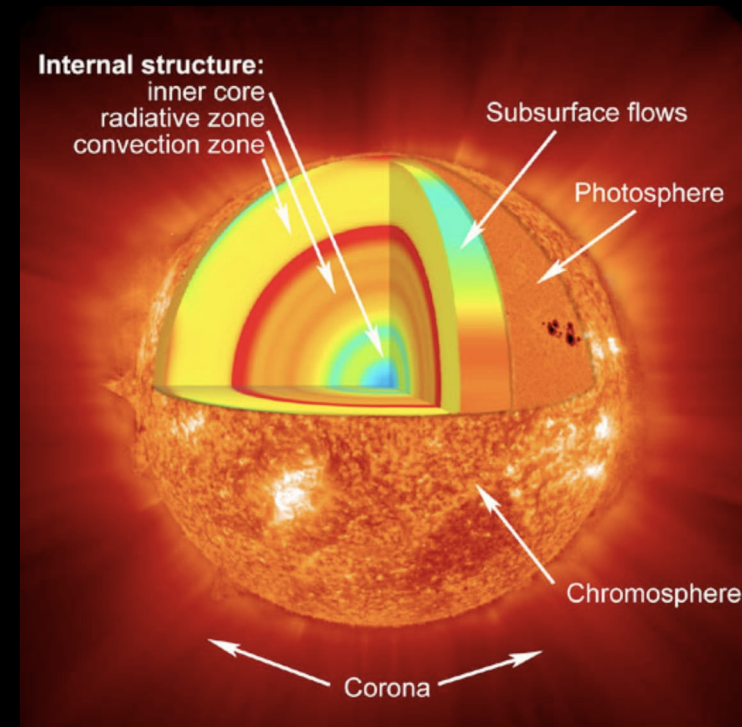
Temperature-reversed region

T : 10,000 K

Corona... 2500 km ~

Hot and low-density region

T ≥ 1,000,000 K



SOHO (ESA & NASA)

Modeling of the Solar Interior

Solar interior (below the photosphere)... invisible with electromagnetic waves

(transparent against neutrinos & acoustic-gravity waves)



Theoretical modeling based on physical laws is required to investigate the internal structure of the Sun.

→ This is done using **stellar evolution theory** combined with **observed data of the solar surface (photosphere)**.

Stellar evolution theory...

describes how the internal structure of a star develops with time

Assumptions (in the case of the Sun):

1) **Spherically symmetric** (solar rotation, global convective flow, and solar magnetic field are neglected)

2) **Chemical composition:** $X(t) + Y(t) + Z(t) = 1$, $Z(t) = 0.017$ (constant)

Fractional abundance: X... hydrogen, Y... helium, Z... other heavy elements

This is the value observed at solar surface.

This is a typical value for population I stars.

3) **Mixing length** (l_{mix}) is introduced to describe the convection zone.

Important parameter values... estimated from the present state of the Sun:

1) **Initial helium abundance...** $Y_0 = Y(t=0) \simeq 0.25$ according to the present Sun's luminosity

2) **Ratio of mixing length to pressure scale height (convection zone)...**

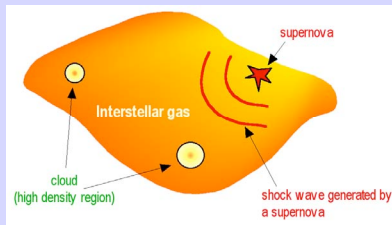
$$\alpha \equiv \frac{l_{mix}}{H_p} \simeq 1 \text{ according to the present Sun's radius}$$

Protostar evolution

How is a star born?

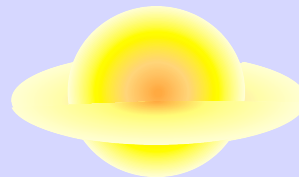
Pre-main-sequence stellar evolution

1) Initial cloud collapse



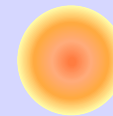
Disturbances produced by, for example, a supernova locally form a high-density cloud in interstellar medium, which then starts to collapse by self gravity.

2) Accretion & dynamic contraction



Interstellar gas in the vicinity of a collapsing cloud continuously accumulates on it (**accretion**) and the cloud rapidly contracts.

3) Slow contraction



After the accretion, the central cloud slowly contracts as a whole (**quasi-static contraction**). During this phase, gravitational energy is converted into thermal and radiative energy (becomes hotter and brighter).

1) Initial cloud collapse ($\sim 3 \times 10^7$ yr)

The distribution of density in **interstellar medium** is subject to disturbances via, for example, a **shock wave produced by a supernova**.



These disturbances locally form a **high-density cloud** which starts to collapse when the **Jeans condition** is satisfied (**gravitational contraction wins gas pressure repulsion**):

$$\frac{G m_c}{r_c} > \frac{R T}{\mu}$$

G : gravitational constant

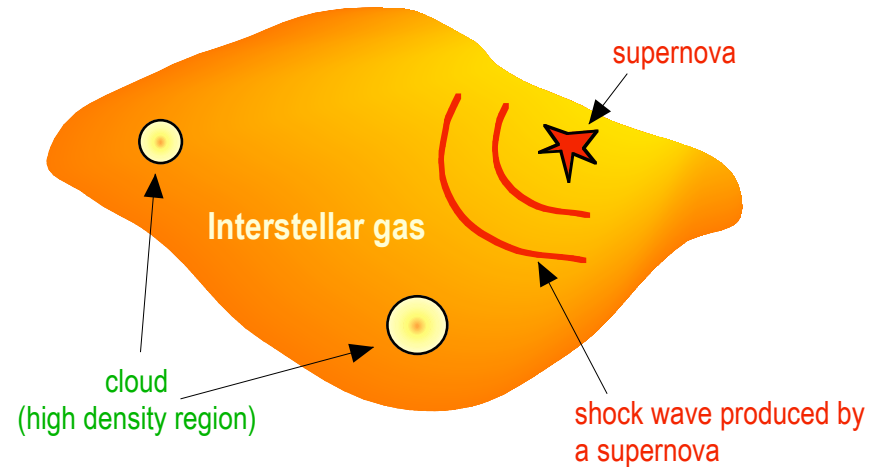
R : gas constant

r_c : radius of a cloud

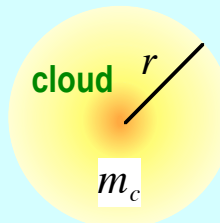
m_c : mass of a cloud

T : temperature of a cloud

μ : mean molecular weight of a cloud



Jeans condition



average density of a cloud:

$$\rho \sim \frac{m_c}{\frac{4}{3}\pi r_c^3} \Rightarrow r_c \sim \left(\frac{3 m_c}{4\pi \rho} \right)^{\frac{1}{3}}$$

$$\frac{G m_c}{r_c} > \frac{R T}{\mu} \rightarrow m_c > \left(\frac{3}{4\pi} \right)^{\frac{1}{2}} \left(\frac{R}{G \mu} \right)^{\frac{3}{2}} T^{\frac{3}{2}} \rho^{-\frac{1}{2}}$$

As collapse goes on (density increases), the lower limit of m_c decreases, so collapse is facilitated (positive feedback... **collapse instability**)

Typical time scale of the collapse... **free-fall time:**

$$t_{ff} \sim \frac{1}{\sqrt{G \rho}}$$

typical density of interstellar gas... $10^{-23} \text{ g cm}^{-3}$
 $\Rightarrow t_{ff} \sim 3 \times 10^7 \text{ yr}$